

# Advanced Investment Analytics

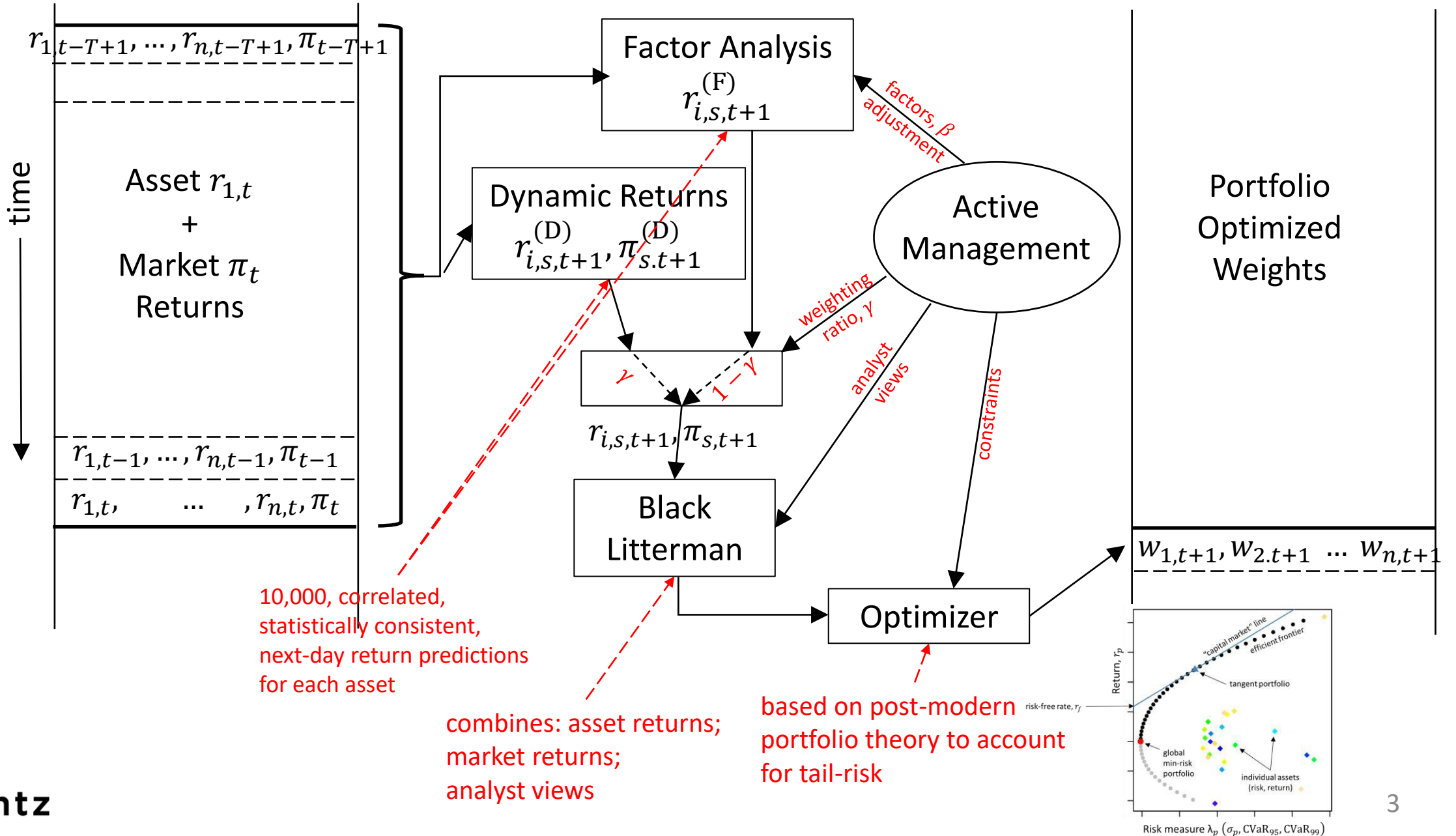


# The Jantz Analytics Platform

An investment platform featuring

1. risk-return sophisticated portfolios, including
  - optimization based upon post-modern portfolio theory
  - dynamic (look ahead) portfolio optimization
  - factor analysis-based optimization
  - Black-Litterman implementation of market and management views
  - the ability to maximize overall ESG rating along with traditional return
  - daily backtesting
2. a suite of risk analytics/tools
  - performance ratios
  - incremental and component value-at-risk
  - statistical factor analysis
  - performance attribute constraints
  - early warning systems
3. derivative pricing based upon arbitrage-free, dynamic asset pricing theory, including
  - improved asset pricing
  - ESG derivative pricing
  - future volatility forecasting based on
    - VIX-like implied volatility
    - “intrinsic time” volatility

# Optimization featuring Dynamic Return Forecasting and Active Management



# Dynamic Return Forecast

asset return

random shocks

**ARMA**

$$r_{t+1} = f(r_t) + h(a_{t+1}, a_t)$$

$f(), h(), g()$  comprise the systematic component of the model for each asset

**GARCH model**

$$a_{t+1} = \sigma_{t+1} \epsilon_{t+1}$$

$$\sigma_{t+1}^2 = g(\sigma_t^2, a_t^2)$$

Jantz Analytics platform pays attention to the random process capturing correlated response of assets to shocks

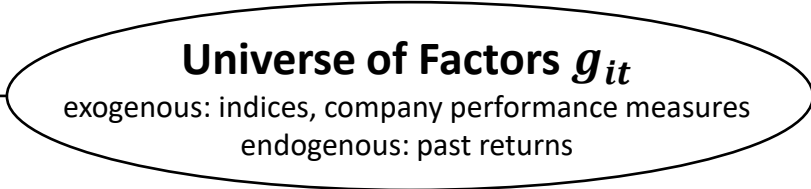
Captures volatility clustering, skewness, & heavy-tails

1. Determine an appropriate multivariate model  $\mathcal{E}$  for the random process  $\epsilon_t$
2. Fit the ARMA-GARCH- $\mathcal{E}$  model to asset return data
3. From the fitted  $\mathcal{E}$  model generate 10,000 scenarios (Basel II accord) of  $\epsilon_{s,t+1}, s = 1, \dots, 10,000$  for each asset
4. Combine the systematic components with the  $\epsilon_{s,t+1}$  scenarios to predict 10,000 return scenarios  $r_{s,t+1}^{(D)}$  for each asset
5. Combine the  $r_{s,t+1}^{(D)}$  scenarios with the scenarios generated by the factor model  $r_{s,t+1}^{(F)}$

$$r_{s,t+1} = \gamma r_{s,t+1}^{(D)} + (1 - \gamma) r_{s,t+1}^{(F)}$$

6. Pass  $\{r_{s,t+1}\}$  to optimizer to generate weights for next day

# Factor Analysis



Test universe for  $k$  factors (MSCI Barra)

Select  $k$  specific factors (Fama-French)

Factor model:  $r_t = \mu + \sum_{j=1}^k \beta_j f_{jt} + \epsilon_t$

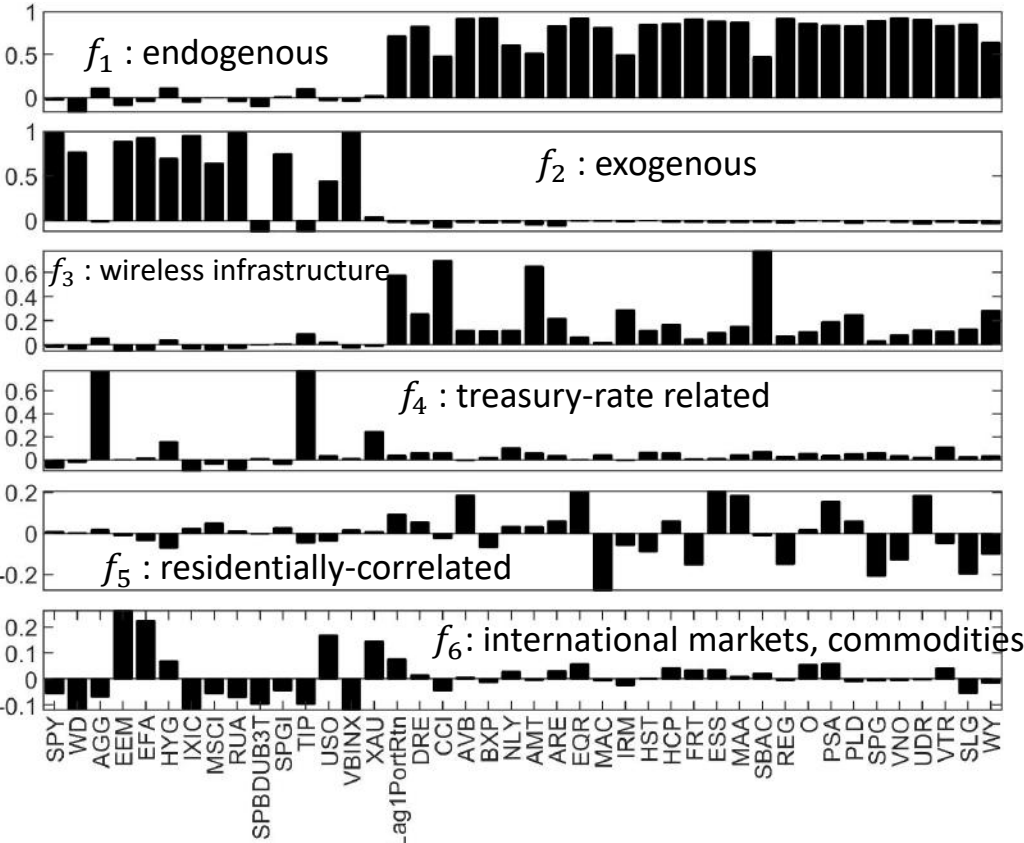
asset return  $r_t$ , mean return  $\mu$ , loadings  $\beta_j$ , factors  $f_{jt}$ , unexplained return  $\epsilon_t$

$f_{jt} = \sum_{i=1} a_{ji} g_{it}$

$$f_{jt} = g_{jt}$$

$$r_t = \beta_0 + \beta_1 EP_t + \beta_2 BP_t + \beta_3 CP_t + \beta_4 SP_t + \beta_5 REP_t + \beta_6 RBP_t + \beta_7 RCP_t + \beta_8 RSP_t + \beta_9 CTEF_t + \beta_{10} PM_t + \beta_{11} FG_t + \epsilon_t$$

- EP: earnings / price      REP: current EP/5yr av EP      CTEF: consensus earnings forecast
- BP: book value / price      RBP: current BP/5yr av BP
- CP: cash flow / price      RCP: current CP/5yr av CP      PM: price momentum
- SP: sales / price      RSP: current SP/5yr av SP      FG: CNN fear & greed index



factor loadings

factor loadings

risk analysis: determine return and risk sensitivity to factors

optimization: to generate predictive returns

## Factor Analysis Return Forecast (cont'd)

Factor model

$$r_{t+1} = \mu + \sum_{j=1}^k \beta_j f_{jt} + \epsilon_{t+1}$$

Existing methods focus on the systematic component of factor model

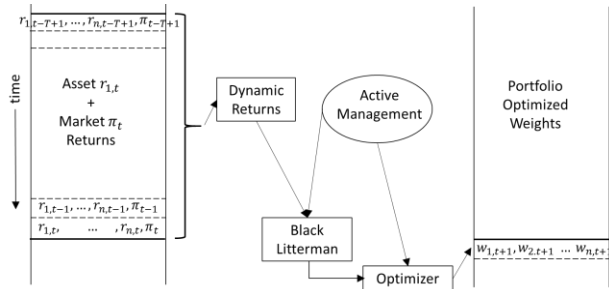
Jantz model does not ignore the stochastic component

1. Perform a time-series analysis of the correlation structure between the  $\epsilon_t$  of each asset
2. From the correlation structure generate 10,000 scenarios of  $\epsilon_{s,t+1}$ ,  $s = 1, \dots, 10,000$  for each asset
3. Combine the systematic component  $\sum_{j=1}^k \beta_j f_{jt}$  with the  $\epsilon_{s,t+1}$  scenarios to predict 10,000 return scenarios  $r_{s,t+1}^{(F)}$  for each asset
4. Combine the  $r_{s,t+1}^{(F)}$  scenarios with the scenarios generated by the existing dynamic module  $r_{s,t+1}^{(D)}$ 
$$r_{s,t+1} = \gamma r_{s,t+1}^{(D)} + (1 - \gamma) r_{s,t+1}^{(F)}$$
5. Pass  $\{r_{s,t+1}\}$  to optimizer to generate weights for next day

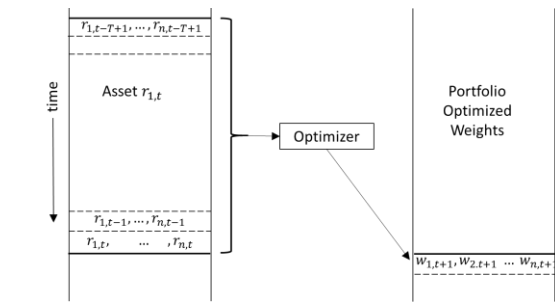
# Dynamic vs Historical Optimization

long-only strategy  
27 U.S. REITs

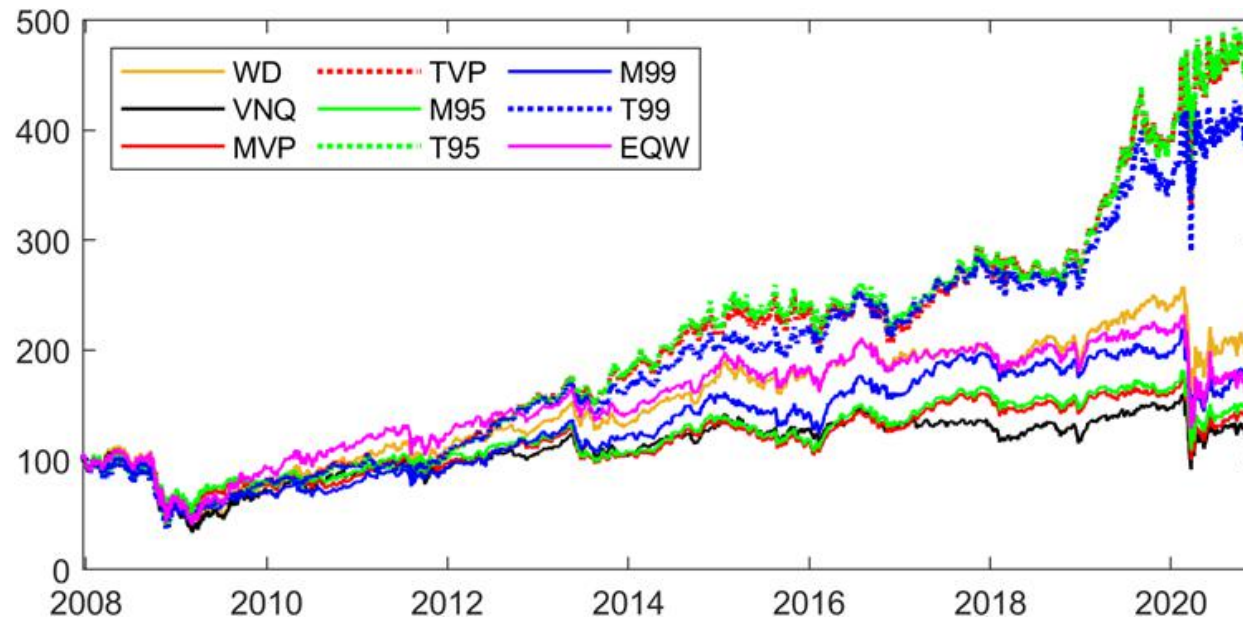
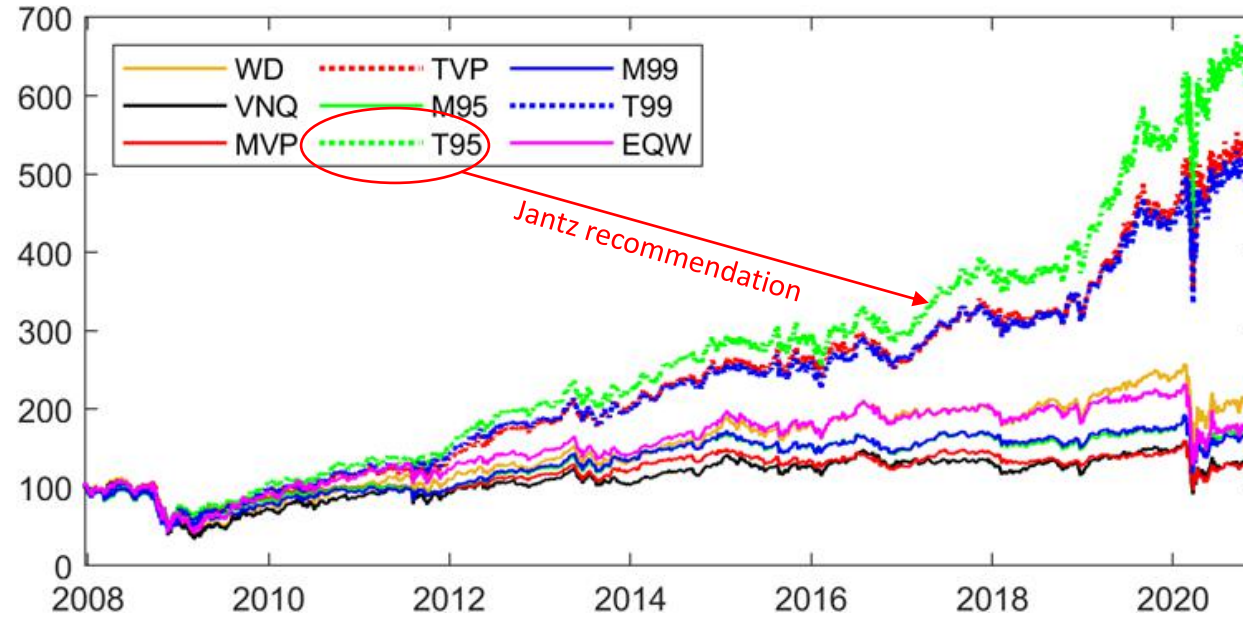
Dynamic



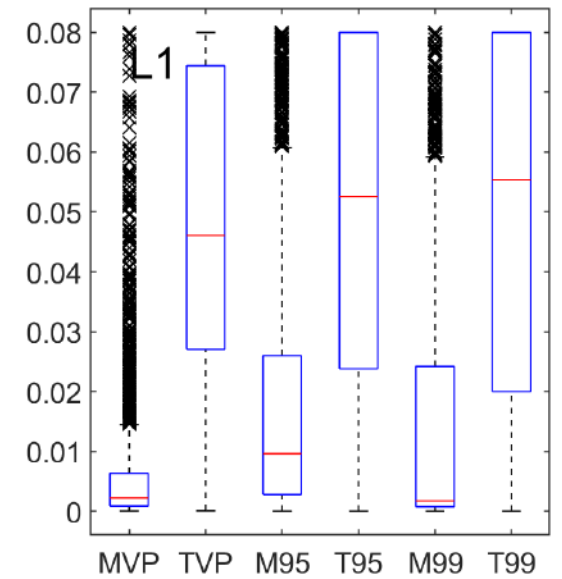
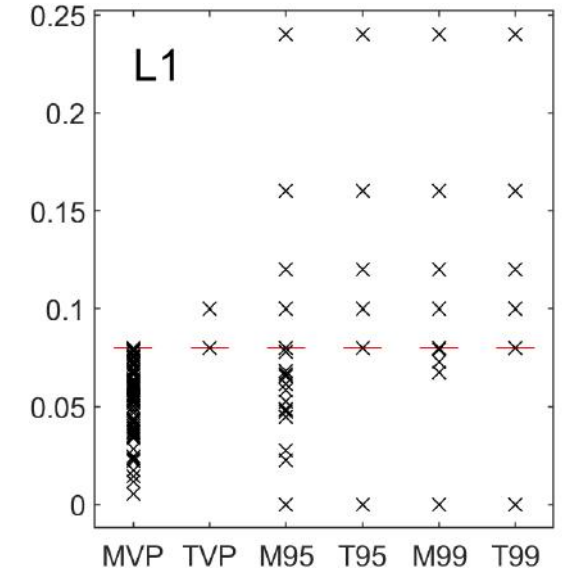
Historical



Cumulative price



Turnover statistics

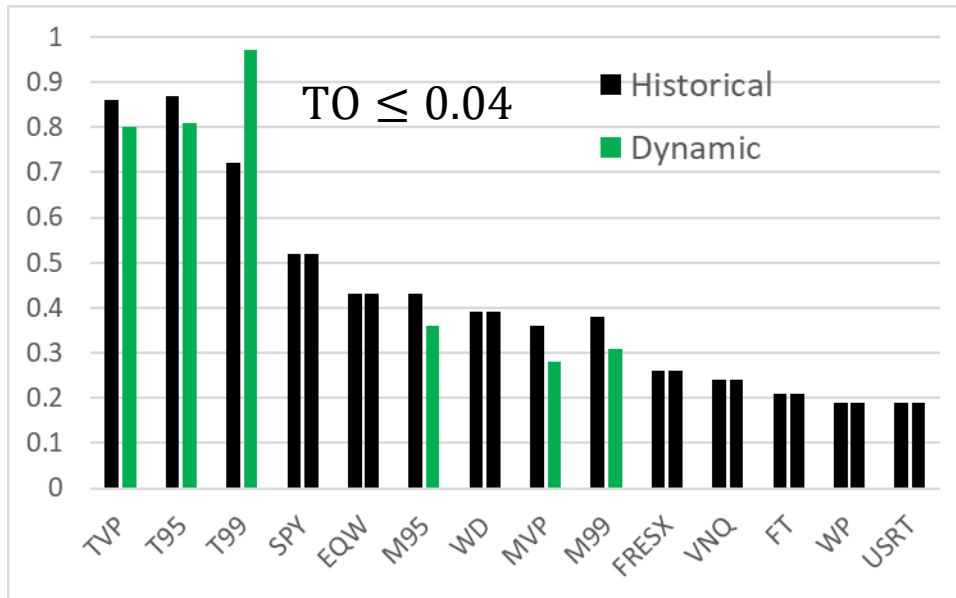
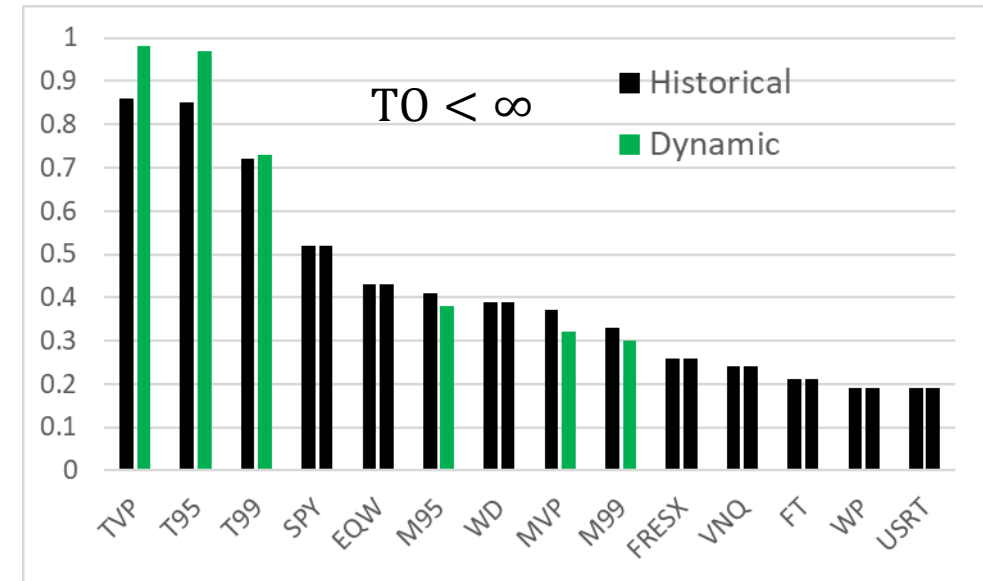


## Performance measures

12/17/2008 – 12/18/2020 average score combined

total return, maximum drawdown, Sharpe ratio, Sortino-Satchell ratio, Rachev ratio

Optimized portfolios compared to benchmarks





## Trend-Persistent\* (Momentum) Strategies for Intraday Trading (27 U.S. REITs)

$\alpha^1$	$L$ (\$)²	Total return (%) period³	ann'd	CVaR⁴	CVoR⁵	MDD⁶
Long-short based on Sharpe ratio, $t_{\text{form}} = 5$ , no optimization						
n.a.	100	17.6	66.6	-0.209	0.225	0.214
Zero investment long-short, cash cushioned						
0.00	200	44.6	220	-0.210	0.223	0.076
0.25	500	129.6	1,277	-0.438	0.466	0.207
0.75	100	20.2	78.8	-0.129	0.133	0.071
0.95	100	22.0	87.3	-0.119	0.126	0.048
Buy and hold (no optimization, no adjustment)						
n.a.	n.a.	19.7	76.5	-0.136	0.1219	0.071
Winner-loser adjusted, long						
0.75	100	23.0	92.2	-0.110	0.110	0.085
0.95	100	23.0	92.3	-0.110	0.110	0.085
Composite: buy & hold + long/short						
0.00	200	24.3	98.3	-0.126	0.120	0.066
0.00	500	27.2	113	-0.125	0.121	0.057
0.25	200	22.2	88.2	-0.129	0.122	0.067
0.25	500	32.8	144	-0.123	0.120	0.055
0.75	1000	35.7	162	-0.140	0.140	0.058
0.95	1000	35.7	161	-0.140	0.141	0.060

\*  $t_{\text{formation}} = 200$  min

$t_{\text{hold}} = 30$  min

<sup>1</sup>  $\max(\alpha E(r_{p,t+1}) - (1 - \alpha) \text{CVaR}_{95,t+1})$

$\alpha = 0$ : minimum risk portfolio

$\alpha = 1$ : maximum return portfolio

<sup>2</sup> Short 3 expected losers @  $-\$L/3$

Long on 3 expected winners @  $+\$L/3$

<sup>3</sup> 1/12/2021 to 5/05/2021

<sup>4</sup> conditional value-at-risk (95% CL)

<sup>5</sup> conditional value-of-return (95% CL)

<sup>6</sup> maximum drawdown over period

buy & hold initial investment \$10,000

## Performance ratios

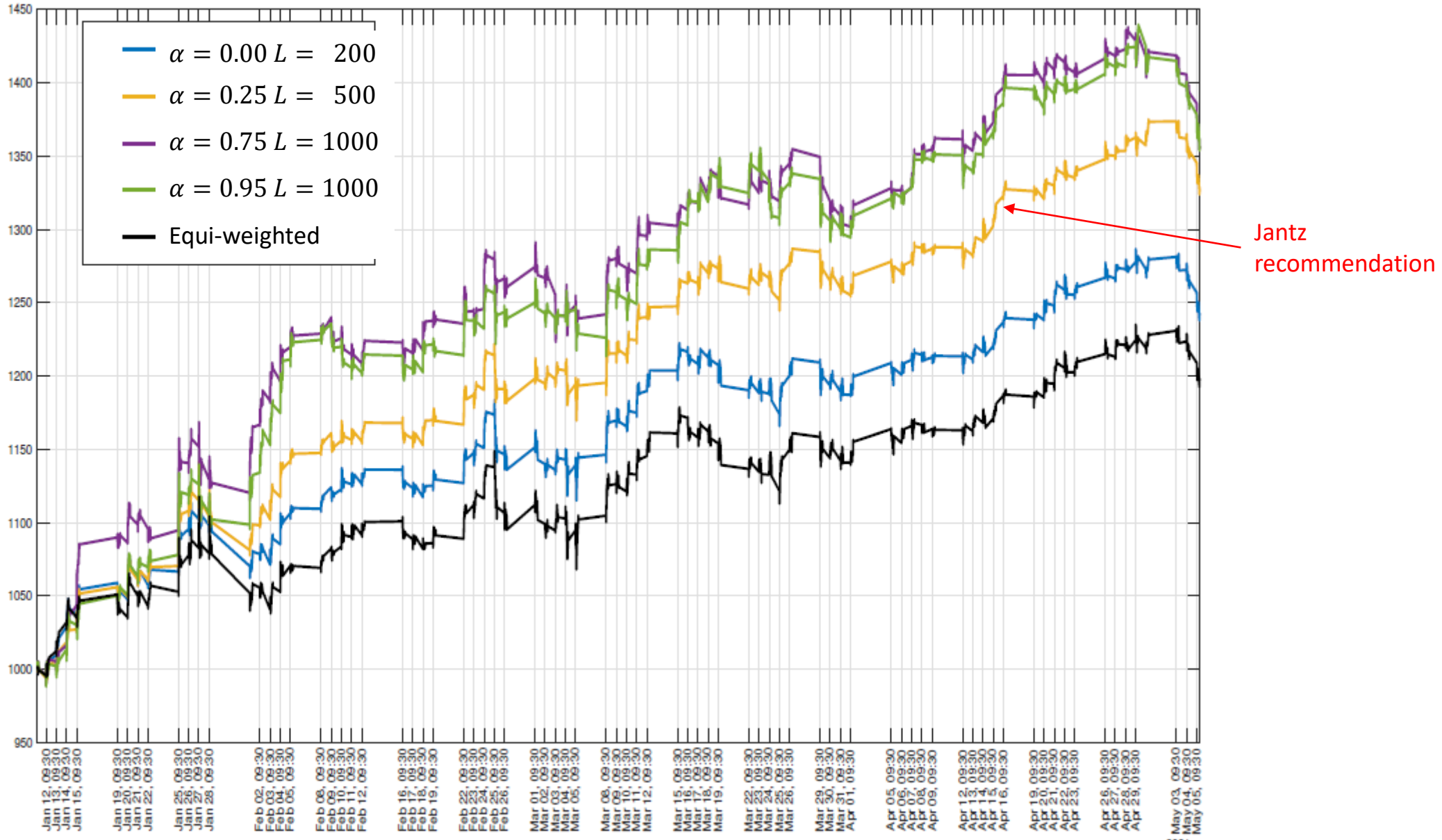
$\alpha^1$	$L (\$)^2$	Sharpe	Sortino	STAR	Rachev	Gini
Long-short based on Sharpe ratio, $t_{\text{form}} = 5$ , no optimization						
n.a.	100	0.51	0.80	0.25	107.4	1.25
Zero investment long-short, cash cushioned						
0.00	200	1.20	1.86	0.58	106.2	2.76
0.25	500	1.26	2.01	0.62	106.5	3.14
0.75	100	0.96	1.46	0.47	103.2	2.26
0.95	100	1.11	1.74	0.55	105.5	2.60
Buy and hold (no optimization, no adjustment)						
n.a.	n.a.	1.00	1.36	0.44	94.6	2.15
Winner-loser adjusted, long						
0.75	100	1.34	1.89	0.62	99.9	2.91
0.95	100	1.27	1.80	0.58	99.3	2.80
Composite: buy & hold + long/short						
0.00	200	1.29	1.77	0.57	95.2	2.81
0.00	500	1.44	2.02	0.63	96.4	3.14
0.25	200	1.18	1.61	0.51	94.5	2.54
0.25	500	1.72	2.42	0.76	97.6	3.78
0.75	1000	1.57	2.27	0.72	100.1	3.53
0.95	1000	1.58	2.32	0.72	100.3	3.51

$$\text{Sharpe} = \frac{E[r_p - r_f]}{\sigma_{r_p - r_f}} \quad \text{Sortino} = \frac{E[r_p - r_f]}{(\sigma_{r_p - r_f})}$$

$$\text{STAR} = \frac{E[r_p - r_f]}{\text{CVaR}_{95}[r_p - r_f]} \quad \text{Rachev} = \frac{\text{CVoR}_{95}[r_p - r_f]}{\text{CVaR}_{95}[r_p - r_f]}$$

$$\text{Gini} = \frac{E[r_p - r_f]}{-\gamma \text{cov}\{(r_p, [1 - F(r_p)]^{\gamma-1})\}}, \gamma = 1.1$$

# Horse-race comparison: Composite: buy and hold + long/short



# ESG Score in Portfolio Optimization (DOW 30)

Maximize  $\left\{ \alpha E \left( r_{p,t+1}^{(ESG)} \right) - (1 - \alpha) \text{CVaR}_{95} \left( r_{p,t+1}^{(ESG)} \right) \right\}$

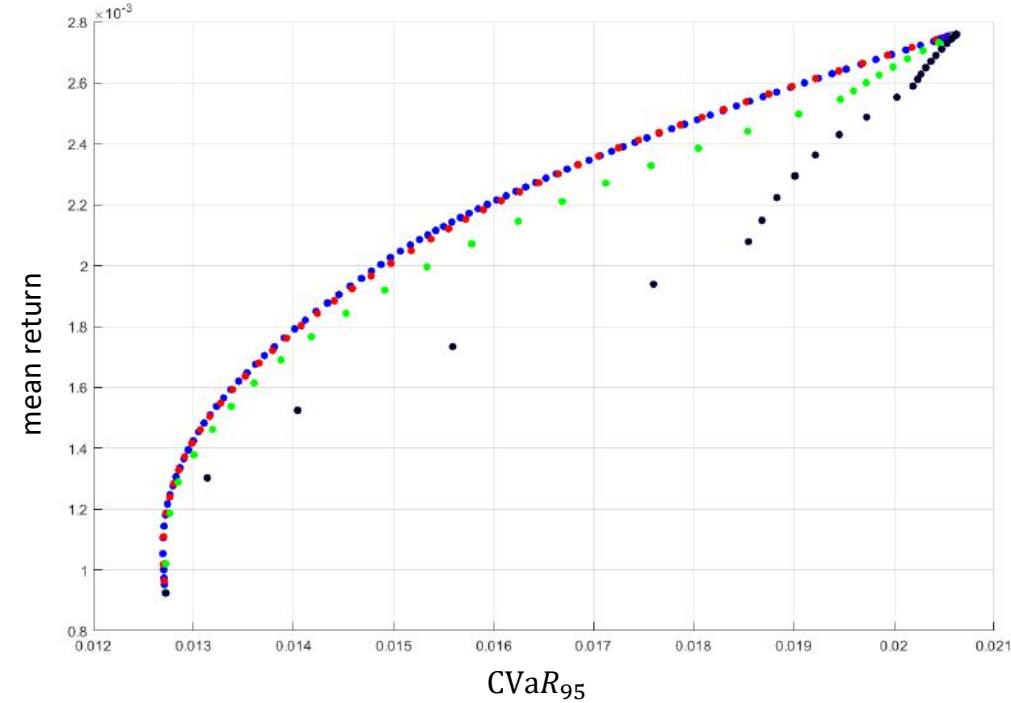
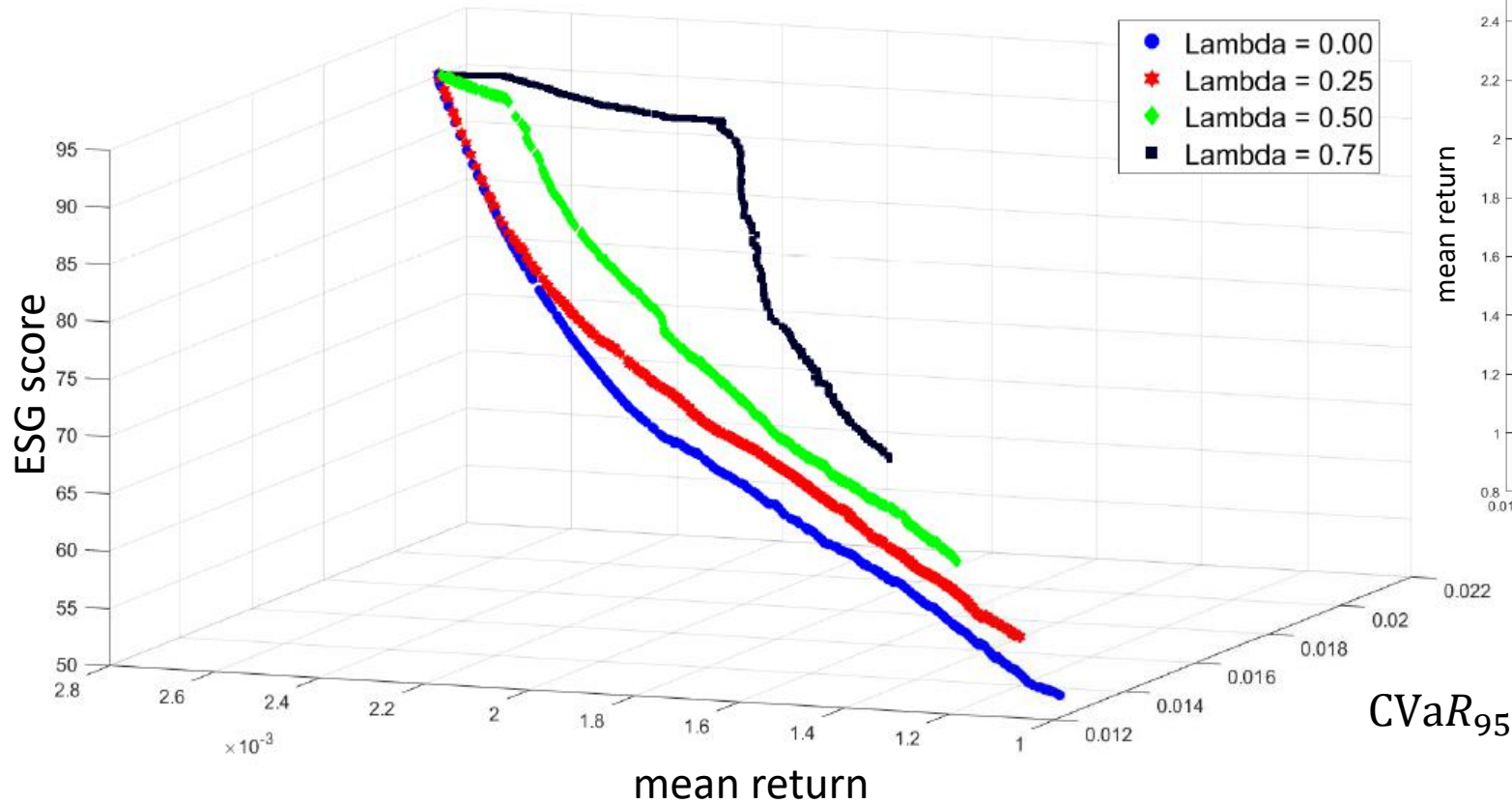
where  $r_{p,t+1}^{(ESG)} = \sum_{i=1}^n w_i \left[ \lambda \text{ESG}_{i,t+1} + (1 - \lambda) r_{i,t+1} \right]$

$V(r_{p,t})$ : portfolio risk measure e.g.  $\text{CVaR}_{95}$

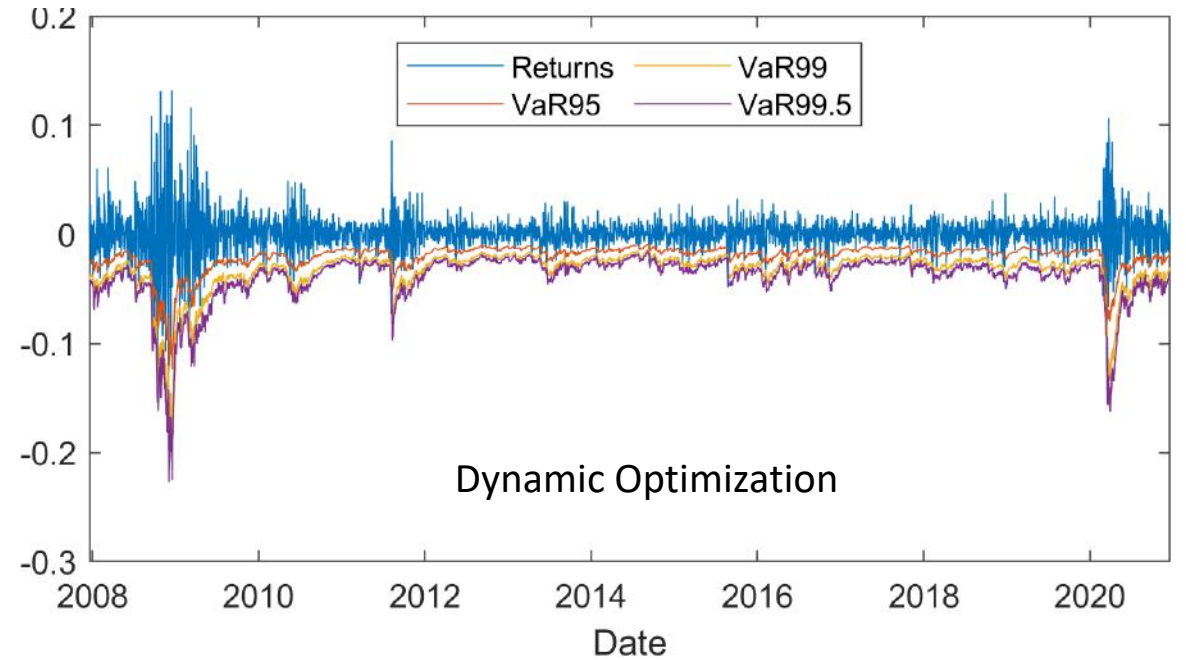
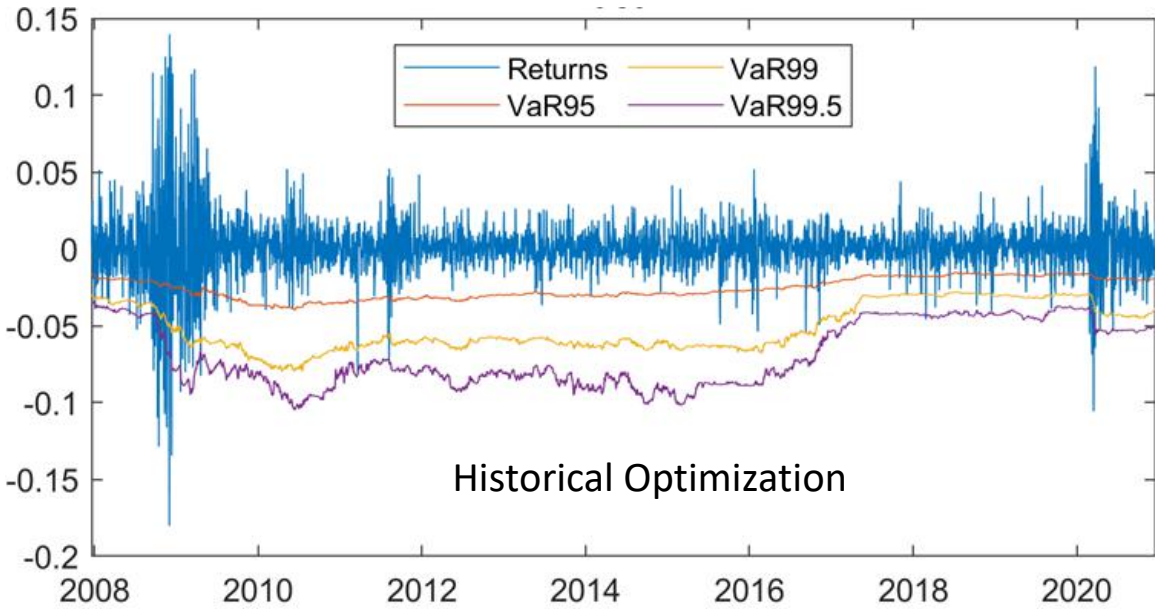
$E(r_{p,t})$ : expected portfolio return

$\Gamma_{i,t}$ : standardized ESG score for asset  $i$

$r_{i,t}$ : return for asset  $i$



# Backtesting (TVP, 27 U.S. REITs)



$1 - \alpha$	TL	BIN	PoF	TUFF	CCI	TBFI	CC	TBF
		$p_{BIN}$	$p_{POF}$	$p_{TUFF}$	$p_{CCI}$	$p_{TBFI}$	$p_{CC}$	$p_{TBF}$
0.95	0.9827	0.035	0.039	0.237	$1.8 \cdot 10^{-8}$	$< 10^{-40}$	$1.5 \cdot 10^{-8}$	$< 10^{-40}$
0.99	1.0000	$6.8 \cdot 10^{-7}$	$9.2 \cdot 10^{-6}$	0.089	$9.2 \cdot 10^{-8}$	$< 10^{-30}$	$3.4 \cdot 10^{-11}$	$< 10^{-33}$
0.995	1.0000	$1.2 \cdot 10^{-5}$	$1.4 \cdot 10^{-4}$	0.041	$1.6 \cdot 10^{-5}$	$< 10^{-25}$	$6.5 \cdot 10^{-8}$	$< 10^{-27}$

$1 - \alpha$	TL	BIN	PoF	TUFF	CCI	TBFI	CC	TBF
	$P(X \leq x N, \alpha)$	$p_{BIN}$	$p_{POF}$	$p_{TUFF}$	$p_{CCI}$	$p_{TBFI}$	$p_{CC}$	$p_{TBF}$
Basel I 0.95	0.979	0.042	0.047	0.237	0.035	$6.810^{-7}$	0.015	$4.010^{-7}$
0.99	0.952	0.103	0.119	0.089	0.017	0.004	0.017	0.003
Basel II 0.995	0.955	0.100	0.121	0.616	0.568	0.123	0.256	0.096

TL – Basel II traffic light test

PoF – proportion of failures (Kupiec, 1995)

CCI – conditional coverage independence (Christoffersen, 1998)

TBFI – time between failures independence test (Haas, 2001)

BIN – binomial test

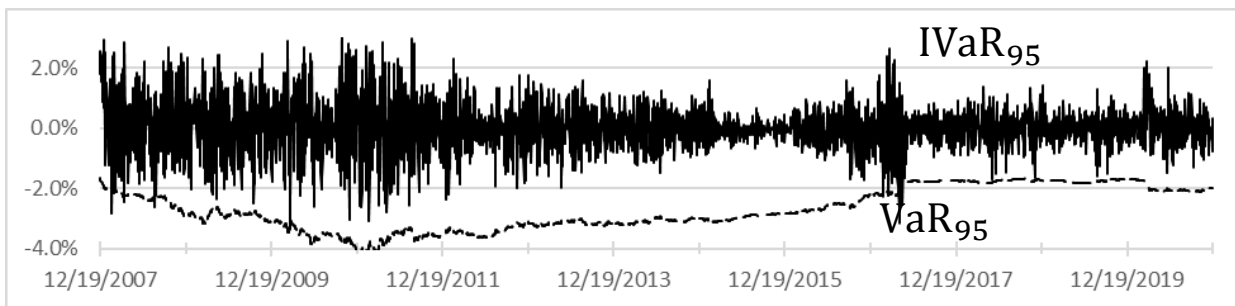
TUFF – time until first failure (Kupiec, 1995)

CC – conditional coverage (PoF + CCI)

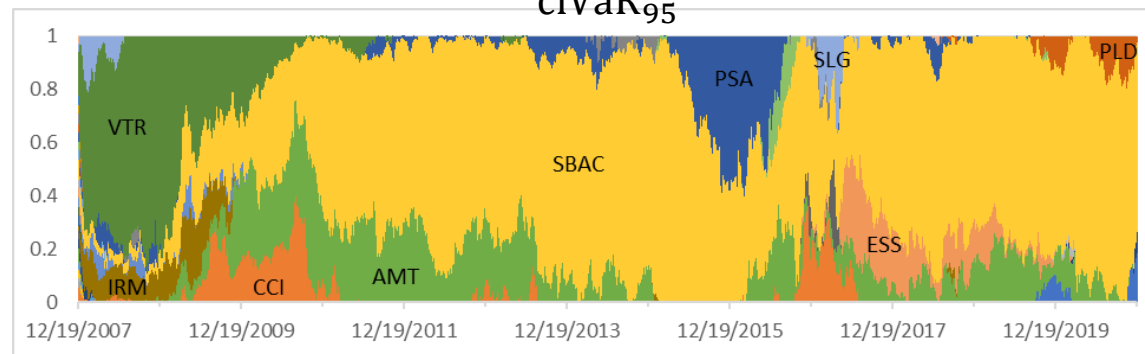
TBF – time between failures (PoF + TBFI)

# Risk Analytics

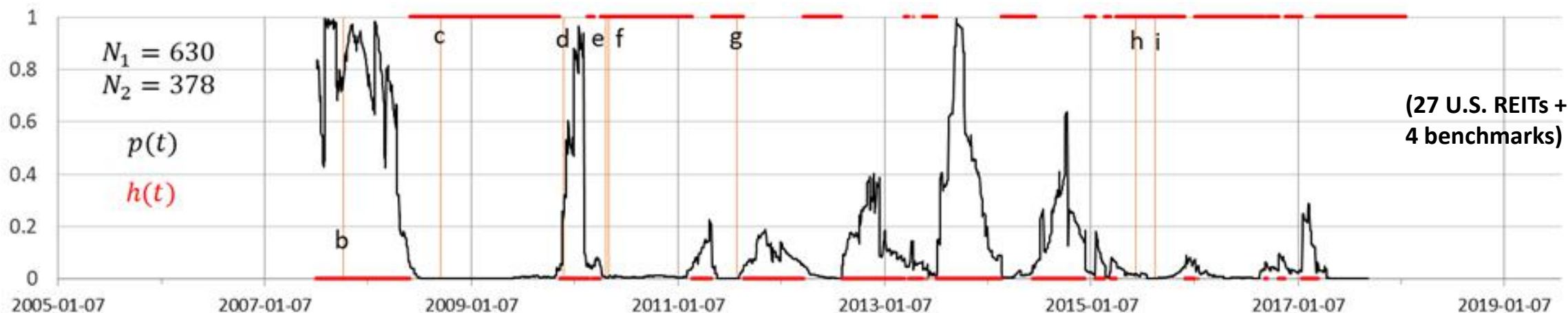
Monitor daily total (VaR), incremental (IVaR), and component ciVaR value-at-risk



(TVP, 27 U.S. REITs)



Early Warning: Search for precursor signals in the correlation structure of assets prior to a shock



Structural breaks detected commensurate with almost every one of the major world market upheavals over this time-period

b: US bear market; c: great recession; d: Dubai debt standstill; e: European sovereign debt crisis;  
 f: US flash crash; g: US Aug 2011 decline; h: China crash; i: US market selloff

# Improved Asset Pricing Intrinsic-Time Volatility

Brownian motion (produces Gaussian, symmetric returns)

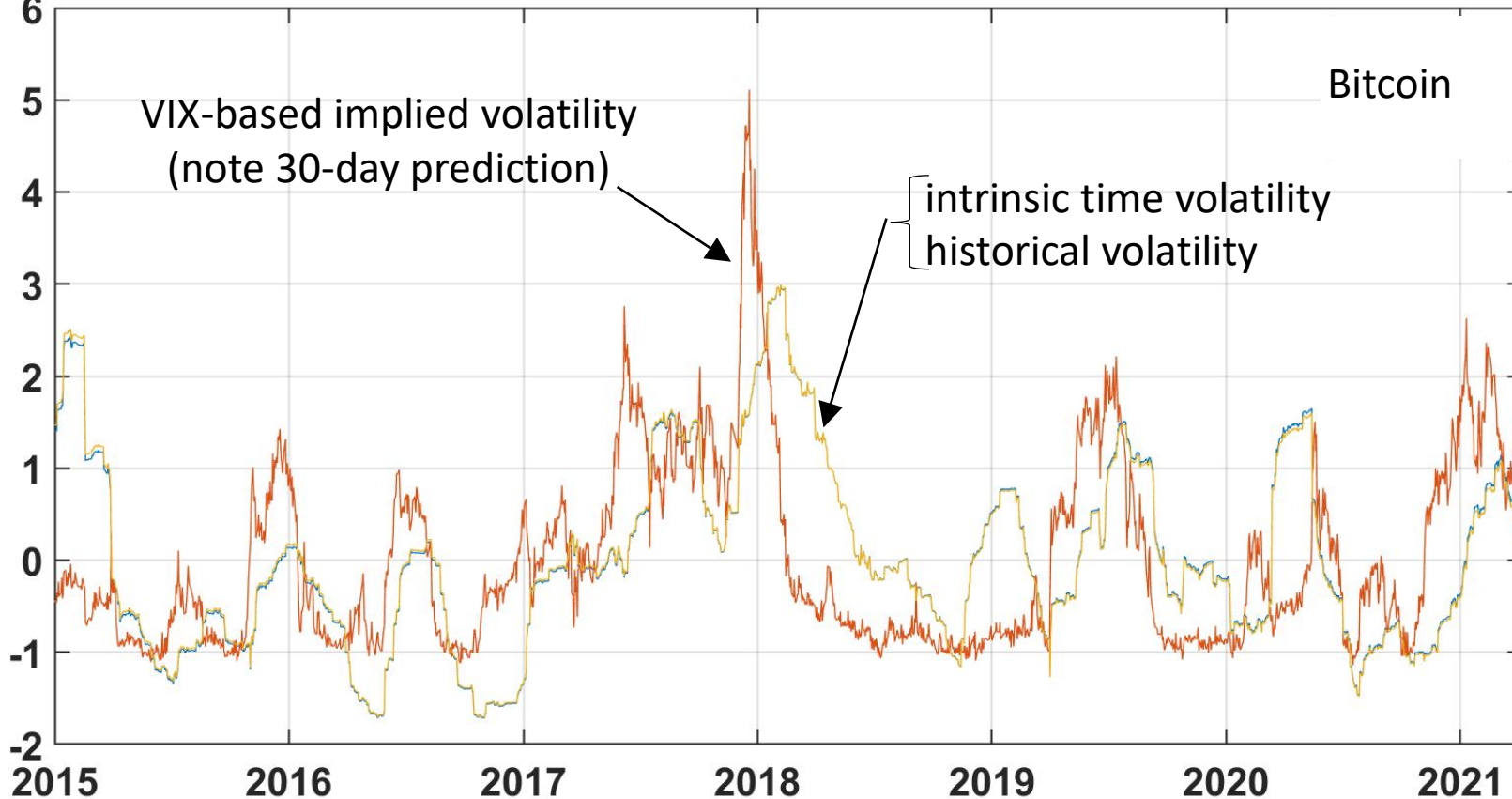


Classic model:  $S_t = S_0 e^{X_t}$ ,  $X_t = \mu t + \sigma B_t$

Double subordination:  $X_t = \mu t + \sigma B_{\mathcal{T}(U(t))}$

subordinated Lévy processes  $\mathcal{T}(U(t))$   
 $\mathcal{T}$  transforms Gaussian returns in unit time  
 → skewed and heavy-tailed returns in unit time  
 $U$  transforms SH-T return events from unit-time spacing  
 → random time (intrinsic time) spacing

$\sigma^2 \rightarrow \sigma^2 \text{Var}(\mathcal{T}(U(t))) \rightarrow$  improved volatility prediction



## To do

- Test momentum intraday strategies on crypto assets and Russell 3000
- Reformulate optimal momentum intraday strategy as a mixed integer programming problem for Dow 30, REITs, cryptos, and Russell 3000
- Implement dynamic factor models for monthly returns for Dow 30, REITs, cryptos, and Russell 3000
- Complete option pricing based on REIT daily returns
- Complete ESG optimization and ESG option pricing for daily returns for Dow 30, REITs, cryptos, and Russell 3000



Thank You

